

IBM Research Report

Device Proposals beyond Silicon CMOS

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1. Introduction

As the end of the silicon evolutionary path nears, alternative devices are being proposed on an urgent basis. Such devices involve different materials such as carbon, III-V semiconductors etc., different geometries such as nanotubes, nanowires and graphenoid sheets, different operating principles involving collective phenomena such as coherent tunneling and ferroelectricity and density of states engineering for band-to-band tunneling FETs. All add to a weird device menagerie that needs some sorting out. These device proposals are mostly not new, but they are enabled by the march of technology and the apparent need for a device that breaks the inflexible switching-energy vs. performance limit of silicon CMOS technology. Meanwhile the goalposts shift continually with the evolution of CMOS technology and system design. Here I will attempt to describe and evaluate the most promising to the most outlandish of these devices in terms of future needs for large scale computation.

2. Industry View

End of CMOS scenarios and successor technologies to CMOS has been the fascination of the semiconductor industry for at least the past decade. Numerous

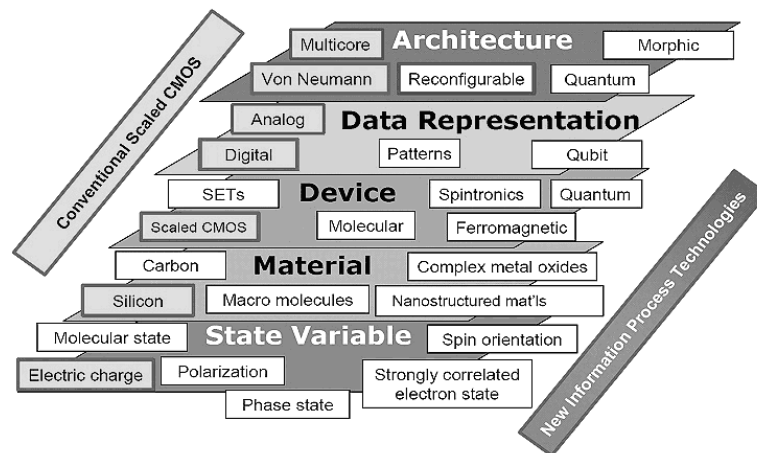


Figure 1. Chart from 2007 International Technology Roadmap, Emerging Research Devices² showing the emphasis on other state variables besides charge for the new information process technologies.

project initiatives and focus centers such as NRI, FENA, MIND, MARCOS etc. have provided support into research on alternative devices, circuits and architectures. So far the lack of success has been notable except perhaps for the RSFQ logic family¹ which is an ultra-high speed superconducting logic family operating at cryogenic temperatures. This logic family has been dropped from the ITRS (2007) menu because working prototypes had been demonstrated but the market had not materialized. The industry view is encapsulated in their chart² reproduced in Fig. 1 with the ‘state variable’ shown at the bottom and proceeding to increasingly higher levels of implementation toward the top (although a strictly 1:1 progression is not implied). A primary motivation exemplified by this chart is to replace the state variable of charge with some other representation (polarization, spin, phase etc.), and the rationale is that a non-charge based state variable may lead to a smaller switching energy since it avoids the electrostatic energy associated with charging the gate capacitance of an FET. Thus we see spintronics features quite prominently in the research efforts as well as propagation of electric or magnetic polarization in quantum cellular automaton type of effects.

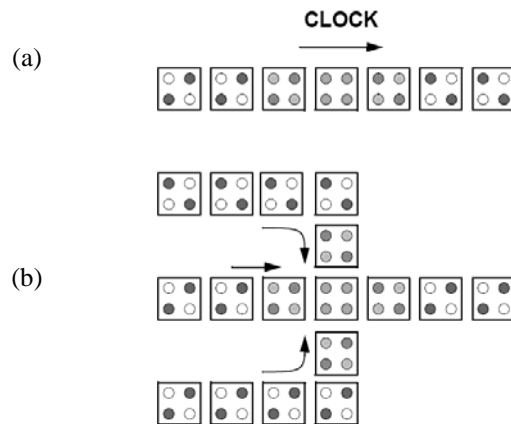


Figure 2. Quantum Cellular Automaton principle, after Lent³: (a) Clock-driven polarization wave propagation along a chain of QCA gates. (b) Majority logic gate where the bottom two inputs determine the output state

Setting aside quantum computation, which is really in a class by itself and won't be discussed here, the proposed solutions fit rather poorly into Von Neumann type architectures, thus research into compatible architectures is integral to assessing the place of some of the more exotic proposals. Much excellent work has been done in exploring these various avenues, and many significant advances have been made, some of which will be discussed below, but so far it seems that the further one strays from the CMOS path (left edge of the chart) the less viable the proposals seem to be. Why is it that CMOS seems to have such an unbreakable monopoly?

While competitors so far have been unable to assault the well nigh impregnable CMOS fortress, CMOS and silicon technology is changing in ways that perhaps can give potential competitors a foothold. With silicon nearing the end of its scaling potential many new solutions are being tried involving an expanding materials inventory. Silicon itself, apart from its role of supporting substrate, is only one layer among many for silicon-on-insulator realizations. Novel self-assembly and hybrid 3-D integration schemes allow the incorporation of other technologies into the silicon mix. Thus the path towards incorporating a novel logic or memory technology is becoming easier.

3. Other State Variables

Computational state variables are simply the physical attributes of a system that carry computational information. The motivation to replace the presently used state variable (voltage, misleadingly called charge) is that the bulk of the energy to switch states (voltages) is used to charge circuit nodes comprising of internal device capacitances, parasitic inter-electrode capacitances and interconnects. Note that the logic is propagated electromagnetically from circuit to circuit at speeds approaching the speed of light. It is the non-local character of the voltage distribution which costs so much in terms of electrostatic energy. Nanoscale CMOS at the 22nm node of the ITRS roadmap has internal switching energies of $\sim 10^{-18}\text{J}$ for a minimum sized device but $\sim 10^{-16}\text{J}$ when including interconnects.

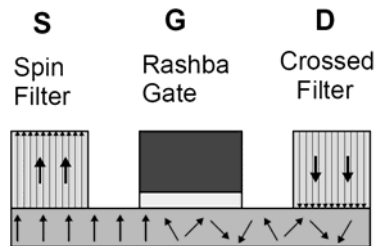


Figure 3. Spin Transistor, after Datta and Das⁷, with crossed polarizers on source and drain . Enhanced spin-orbit coupling due to the gate field promoted rapid thermalization of the injected spins and thence transmission of a portion into the drain.

There is some confusion, as evidenced in Fig. 1, between the above definition and the use of ‘state variable’ such as charge to describe the internal state of a logic switching device. In conventional devices this relationship is not 1-1 since the internal charge is a function of device size, circuit design etc. An abrupt change of state is desired, controlled by a small change of the terminal voltages, which is why collective and strongly correlated states are being sought in new devices.

When an internal state variable is used to directly represent digital bits it is called a token. Information processing occurs by physically passing the token from device to device. This system is attractive because of the isomorphism between the state variable and the logic state heralds perhaps a greater energy efficiency compared to the conventional approach and perhaps a more robust representation compared to the arbitrary nature of voltage representation.

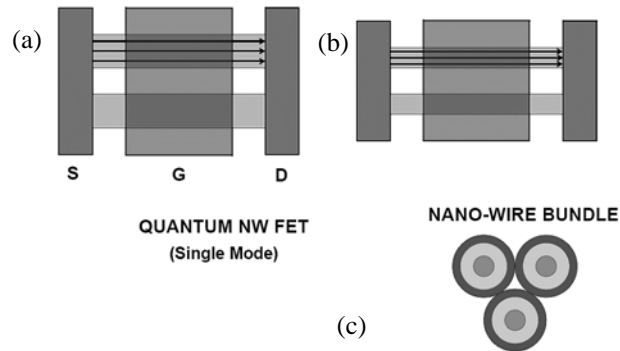


Figure 4. Nanowire scaling: Shrinking width of nanowire (a) to (b) compresses the same amount of active charge into a smaller width therefore increasing the ratio of active to parasitic capacitance. (c) Reduction of parasitic capacitance by nanowire bundling.

The token-carrying logic is exemplified by the QCA (Quantum Cellular Automaton)³ approach as shown in Fig. 2 where the states are represented by two diagonal alignments of internal polarization. The states are separated in energy by several kT , yet transitions can be propagated from cell-to-cell by means of a traveling wave generated by external clock electrodes which adiabatically facilitate the dipole rotation by compensating for the internal potential so that the cell polarization may be driven by weak neighboring fields. An instructive example was recently given for a magnetic QCA⁴⁵. Calculations of energy dissipation for adiabatic transitions (slowly variable field) for flipping of electric and magnetic polarizations^{3,4} and spins⁶ show that it may be very small, much less than kT . Efforts so far on the token passing logic have focused naturally on demonstrations of proof of concept, some with notable success³ but a set of more fundamental questions remain.

Compared to electromagnetic propagation, the speed of propagation of the tokens is much less, typically by $\sim 10^3\times$, also logic interactions are predominantly via neighboring cells (cellular automaton). This gives rise to the following set of questions which to date have not been satisfactorily been addressed: 1) Cellular automata have inherent limitations and inefficiencies in implementing general purpose logic which would result in some penalty factor vis-à-vis CMOS. 2) Many state transitions are utilized for communication rather than logic, which would result in further penalties. 3) How does the communication penalty associated with token passing limit applications? 5) The reactive power for such a system will be very large (creating the propagator fields) so that very high Q clock power supplies will be needed to maintain efficiency, but at present there are no solutions for this.

A family of proposed devices use state variables other than charge to modulate their switching characteristics while still using external voltage and current for logic propagation. These include the Das-Datta spin transistor^{7,8} (see Fig. 3) where the gate modulates the spin lifetime, the Mott transition,^{9,10} quantum correlated states,¹¹ quantum interference devices etc. The device itself needs to be a two-way transducer, converting from the terminal voltages to the internal state variable and back again. The advantages of changing state variable, for instance a claimed lower operating voltage for the spin-transistor, have to offset losses in the transducer chain, and this has been difficult to achieve.

4. Scaling

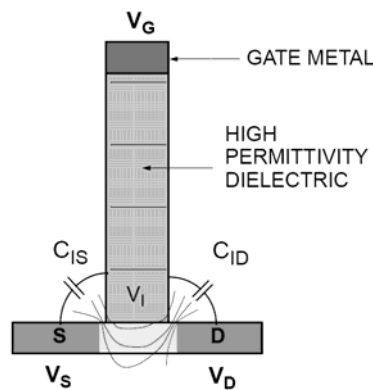


Figure 5. Field effect transistor with a very high permittivity gate dielectric where the gate dielectric thickness may be much larger than the channel length. C_{IS} and C_{ID} are the gate fringing capacitances to source and drain respectively.

Capacitance scales inversely with distance and density with area so that scaling capability has always been an important and desirable characteristic for all new device proposals. The electrostatic QCA, for instance, has the ability to scale all the way down to molecular dimensions. Scaling has of course been extensively discussed elsewhere, but here we will briefly touch on aspects of new devices which make them interesting from the scaling perspective. Even the more conventional technologies are exploring quantum-confined geometries such as nanowires and nanotubes. These confer scaling advantages as a result of reduced dimensionality much like those conferred on 1-D quantum confined lasers. For instance, as illustrated in Fig. 4, 1-D quantum confinement collapses transverse the density of states into a single quantum number (not counting degeneracy), so that the current carrying capacity of the quantum channel is independent of device cross-section. Thus carbon nanotubes can be scaled below 1nm diameter and are still capable of carrying twice (for band degeneracy) the full quantum of conductance, $2e^2/h$, times supply voltage worth of current ($\sim 20\mu A$). Some shibboleths may fall by the wayside, such as the need for the gate to always be in close proximity to the channel of an FET. As illustrated in Fig. 5 it may be possible use highly polarizable materials to

transmit potentials into small devices¹² (see Fig. 5), or even molecules¹³, to control their switching. Another exciting possibility is to use collective effects to suppress single electron tunneling and reduce lateral dimensions. Some work on oxide semiconductors, while still open to interpretation, has shown control of device properties on an extremely small scale.¹⁴

5. Beating $kT(e)$

Table I - Physical Constraints

Energy	Voltage	Distance
kT	kT/e	h/p
Thermodynamic constraint for irreversible computing.	Consequence of charge on single electron.	Consequence of mass of single electron.
Work-Around		
Reversible Computing	<ul style="list-style-type: none"> ▪ Energy Filtering ▪ Spin Filtering ▪ Collective Effects 	<ul style="list-style-type: none"> ▪ m^* engineering ▪ Collective Effects

At this point in the evolution of integrated computing the overwhelming concern is power reduction or, in terms of individual device properties, the energy stored or dissipated per switching event. With today's numbers of transistors per chip at ~1 billion, total power constrained to below ~1W and frequencies in excess of 1GHz, average switching energies need to be below 10^{-17} J per transistor, and these demands will increase exponentially with time. As Table I shows, there is a distinction between switching energy, kT , and the energy per electron, kT/e . The former places an absolute limit on the energy cost of non-reversible computation,¹⁵ while the latter places a restriction on power supply voltage as applied to electron-barrier controlled devices such as FETs. i.e. for a given off-on current ratio r a switching voltage, $V = (kT/e) \ln r$ is required. This is the famous '60 mV/decade' subthreshold slope problem, and much research effort, funded by a dedicated government program, is devoted to finding devices with steeper than 60mV/dec. slopes. This voltage requirement, coupled with the fact that the capacitance per unit length of the interconnects is a constant ~1 times the permittivity of the dielectric, means that switching energy, $\frac{1}{2} CV^2$, is rather insensitive to technology changes¹⁶ depending only on the general length scale. To reduce switching energies therefore requires device, circuit and architectural innovation in addition to scaling. Here we will focus on device innovation. As discussed in a previous paper in this series¹⁷ carbon-nanotube FETs may enable improved switching energies compared to CMOS simply by virtue of their higher performance, therefore offering a better power-performance trade-off, but to go beyond this requires devices operating on different principles.

Table I lists various 'work around' solutions, both to the 60mV/dec. problem and also to the fundamental ' kT ' limit. The latter limit only applies to irreversible operations i.e. all conventional computation, but the token-passing kind of logic

including QCA with electric or magnetic dipoles, and spintronics generally postulate a reversible mode of computation where the clock is varied adiabatically and much of the energy can be recovered (notwithstanding the questions we posed earlier). CMOS logic can, in principle, also be run in a reversible or partly reversible manner¹⁸ but the technical obstacles to achieving significant energy savings are daunting.

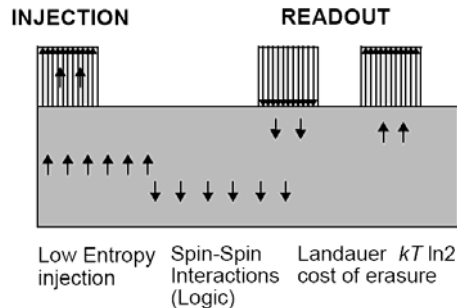


Figure 6. Device with spin polarizers for injection and readout. The spin transport medium has zero bandgap for spin-spin interactions. The readout electrodes have to be biased at a sufficient potential to prevent back injection.

The kT and kT/e limits may be circumvented simply by reducing temperature, and this approach has a long history¹⁹, but in the end refrigerator inefficiencies and the Carnot factor have to be taken into account. Much has been made of the fact that electronic spin interacts weakly with the thermal bath therefore may achieve lower energy dissipation⁶. An illustrative scheme is shown in Fig. 6. Spins polarized electrons are injected into a non-magnetic semiconductor via a polarizer. In the semiconductor the spins may be flipped by weak fields involving voltages of $\ll kT/e$ and may interact with each other to do logic. In reality what we have here is a refrigerator, since the injected spins have a super-cooled distribution in the zero-magnetic gap semiconductor²⁰. Logic can be performed as long as execution times are much shorter than the thermalization time, and the electrons may be extracted (read) via a similar polarizer at no energy cost. However any electrons where the spin has been flipped, either intentionally or through interaction with the thermal bath, will have to be extracted via a complementary polarizer, but to prevent back-injection of the opposite spin polarization and hence contamination of the distribution, this polarizer has to be biased at a voltage of several kT/e with respect to the original injector. From this it is clear that the Carnot penalty is paid back (at least) during this extraction process. It may be justifiably argued that this constitutes a very compact and efficient refrigerator, but remember that this scheme is incomplete since only one degree of freedom (spin) has been cooled this way.

Practically the kT/e limit is more important than the kT limit since voltage and interconnect capacitance place switching energies today above $10^4 kT$ and this

places emphasis on strategies to increase the sharpness of the switching transition, two of which are given in Table I, energy filtering and collective effects. These will be dealt with in the following sections.

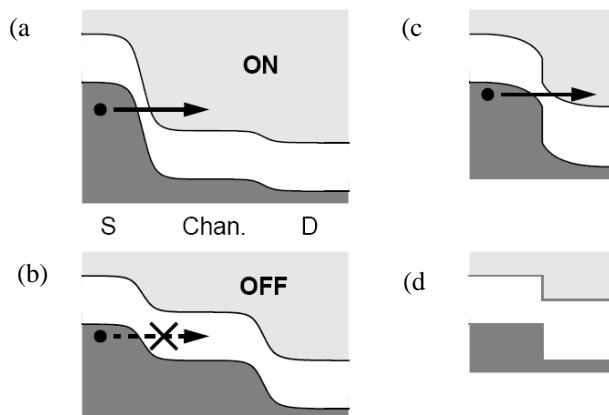


Figure 7. Operating principle of a tunnel field-effect transistor, after Apenzeller²²: (a) The bands are crossed in the 'on' state and (b) uncrossed by the gate voltage in the 'off' state. A staggered gap heterojunction (c) and (d) achieves a small bandgap for tunneling while allowing a larger bandgap in the source and channel regions.

6. Energy filtering

The principle of energy filtering is outlined in a previous paper²¹ and indeed can be traced back to the Esaki diode. The principle, as applied to an n-FET, is illustrated in Fig. 7. When the FET is in the 'on' state electrons originating in the valence band of the p-type source tunnel into the conduction-band of the channel. The device is turned off by raising the conduction-band edge in the channel above the valence band edge in the source. One can say that the Fermi tail of the electrons in the valence band has been cut off above the valence band edge permitting a steeper than 60mV/dec. subthreshold slope. While the principle is clear achieving a steep slope in practice has been difficult and so far has only been demonstrated unambiguously in a carbon nanotube geometry,²² and only at low currents, unsuitable for high-speed devices. Band-to-band tunneling transmission coefficients decrease exponentially with $m_r^{1/2}$ and $E_g^{3/2}$ where m_r is the reduced effective mass for tunneling and E_g is the band gap. Thus materials with small m_r and E_g are desired. A direct bandgap is also important to achieve large current levels. Materials such as carbon nanotubes, graphene ribbons,²³ III-V semiconductors and Ge (almost direct) have the required properties.

Incorporation of heterojunctions²⁴ as shown in Fig. 7b can provide the correct band line-up for the desired tunneling while suppressing tunneling where it is not wanted, such as from the drain into the channel. Nanowires (or nanotubes), with wrap-around gates, are the preferred geometry since this provides an intimate electrostatic control of the tunnel junction by the gate.

7. Band Structure Engineering

While conventional device design has assumed the band structure as a given (e.g. bulk silicon), quantum effects on the Nanoscale can alter band-energies. This may be exploited, in the case of graphene, to make nanoribbons with controlled band-gaps as in proposals for the tunnel FET.²³ For graphene nanoribbons of a certain type the dispersion of edge states (see Fig. 8) may be controlled by a lateral field and this dispersion-modulation has been proposed as a new way of modulating the current²⁵ since transport can occur only when there is finite dispersion. Similarly, other proposals exploit the ability of a perpendicular field to modulate the bandgap of bilayer graphene.²⁶

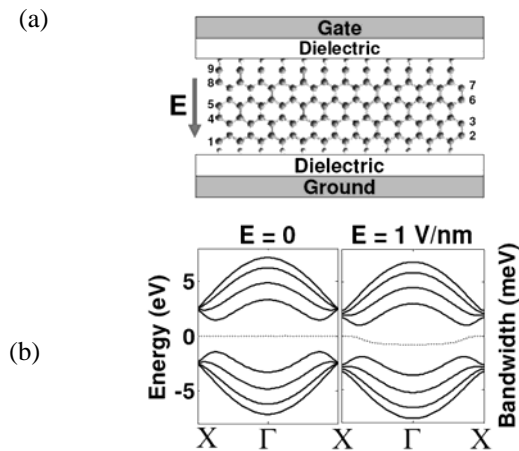


Figure 8. Bandwidth modulation FET, after Raza²⁵: (a) A lateral gate is applied to a graphene nanoribbon. (b) The gate field breaks the symmetry and develops a finite bandwidth to the midgap edge states.

8. Collective Effects

Going back to Table I, the kT/e potential can simply be replaced by kT/ne where n is much larger than unity. i.e. collections of correlated particles still have mean thermal energies of $\sim kT$ but a much lower electric potential than kT/e (As seen in Table I, increased n also offers potential scaling benefits since it reduces h/p). Collective effects are being evoked to extend devices beyond CMOS where dimensions are on the 10nm scale. A legitimate question therefore is how do the collective effects withstand scaling where n decreases perhaps as fast as the cube of the dimension. In the case of ferromagnetism experiments and theory indicate that scaling down to $\sim 5\text{nm}$ is possible^{1,27} and experiments on semiconducting oxides¹⁴ show effects persisting on the $\sim 2\text{nm}$ distance scale.

This can be exploited in switching ferromagnetic or ferroelectric domains, in the Mott metal-insulator transition, in correlated electron condensations such as bilayer graphene²⁸ or semiconducting oxides²⁹ and in correlated tunneling. In addition to the number effect, there are also quantum exchange interactions which reduce potential energies and can give rise to a 'negative capacitance'³⁰, and by in-

ference to switching behavior. As is seen from the above list the field is rich and just beginning to be explored. Here we will follow just two examples of current research interest.

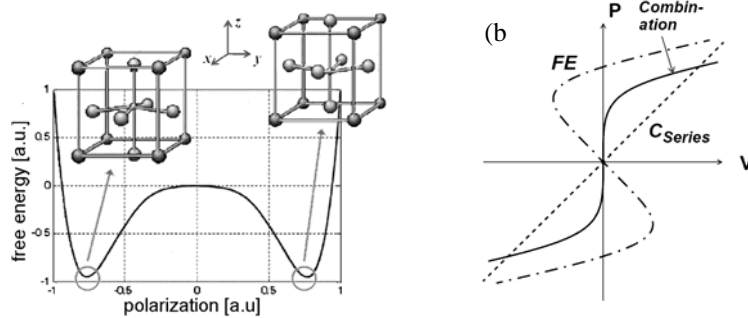


Figure 9. Ferroelectric element (a) in series with the gate of an FET. (b) The ferroelectric response [derivative of (a), highly idealized] is added to the response of the series gate capacitor designed to maximize the change in polarization to small changes in gate voltage. After Salahuddin³¹.

Ferroelectricity leads to hysteretic charge vs. voltage characteristics (analogous to the well known hysteretic loops of ferromagnetism). This is being exploited commercially for memory applications and it has also been proposed for logic devices as a way of increasing the subthreshold slope³¹. It is proposed that by combining the negative capacitance of an unstable ferroelectric state (see Fig. 9) with the positive gate capacitance an FET, that the system may be made marginally stable with the internal gain resulting in an almost vertical off-on transition. The viability of this idea involves many questions concerning domain formation, gain per unit volume, speed etc. Similar proposals are in place for a purely electronic negative capacitance resulting from strong quantum mechanical exchange effects³⁰ as have been seen in oxide semiconductors. Ferromagnetism itself may be used for logic as we have discussed in the case of the magnetic QCA. Also, ferromagnetic spin-wave logic³², is being explored. Research is also being done into multiferroics, especially composite coupled systems,³³ where electric fields may control ferroelectric properties and vice versa.

The other example involves inducing correlated tunneling across two graphene layers²⁸ separated by an insulator, as shown in Fig. 10. When the ‘nesting’ condition is achieved i.e. the electron and hole Fermi surfaces on the two sides are matched, correlated tunneling can occur and the resistance between the two layers is reduced from an insulator-like value to just the quantum of conductance. The remarkable prediction is that the conductance in the ‘on’ state is just the quantum of conductance $2e^2/h$, i.e. it does not depend on the insulator thickness even though uncorrelated tunneling current is thus reduced exponentially. This state has not been found yet, still a device proposal has been advanced³⁴, claimed to operate at

low voltages, drawing analogies between this transition and the superconducting Josephson junction.

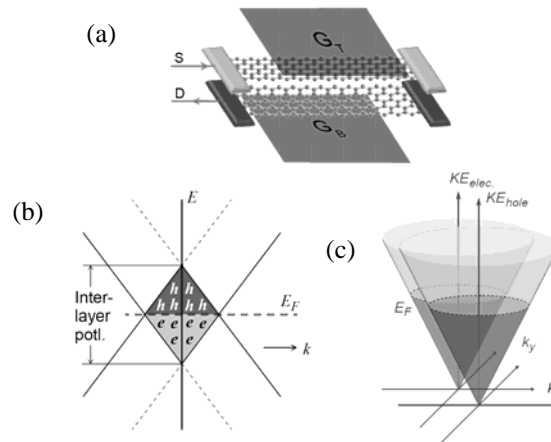


Figure 10. Bilayer PseudoSpin Field-Effect Transistor, after Banerjee³⁴. (a) Two graphene sheets separated by an insulator and gated by top and bottom gates. (b) Bands of the two layers shifted by the gate induced potential achieving the 'nesting' condition, (c) where the electron and hole Fermi surfaces coincide, for correlated tunneling between the layers

9. Outlook

In the above treatment we have tried to convey a flavor of the many approaches used and avenues being investigated to come up with a future device that is better, mainly in terms of power dissipation, than CMOS. Much has been left out and much worthy work left unmentioned, due to lack of space and lack of personal familiarity. For this I apologize. Most of the approaches have not yet resulted in working demonstrations, let alone being competitive. This does not in anyway diminish the quality and importance of this work, since truly a new frontier is being explored and only those in the future, looking back will be able to evaluate the fruits of today's efforts.

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