

# IBM Research Report

## Tunneling Spectroscopy of Two-State Systems

**J. A. Gupta, C. P. Lutz, A. J. Heinrich, D. M. Eigler**

IBM Research Division  
Almaden Research Center  
650 Harry Road  
San Jose, CA 95120-6099



Research Division

Almaden - Austin - Beijing - Haifa - India - T. J. Watson - Tokyo - Zurich

## **Tunneling Spectroscopy of Two-State Systems**

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### Abstract

We observe gap-like and negative differential resistance features in tunneling spectra resulting from transitions between states of H<sub>2</sub> in the junction of a low-temperature scanning tunneling microscope. We develop a model for the conductance of a saturable two-state system where transitions are driven by inelastic scattering of tunneling electrons that explains the distinctive lineshapes of these spectral features and can provide information on the residence times in each state.

In the emerging field of molecular electronics (1), two-terminal measurements with scanning tunneling microscopes (STMs) enable study of the electronic properties of single molecules and atoms in a controlled environment. Such studies have revealed that electronic transport on the atomic scale can strongly depend on atomic or molecular motion (2-3), resonant tunneling through localized states (4), and molecular conformation changes (5).

Here we study tunnel junctions comprising an STM tip, a flat metal surface, and H<sub>2</sub> molecules. Within a range of H<sub>2</sub> surface coverage, differential conductance ( $dI/dV$ ) spectra reveal gap-like and negative differential resistance (NDR) features. By directly resolving two-state noise in the tunnel current, we can attribute these features to transitions between states of H<sub>2</sub> that are driven by inelastic scattering of tunneling electrons. The threshold voltages for transitions increase with H<sub>2</sub> coverage, depend on tip-sample separation and do not match known rotational or vibrational modes. We develop a model for a two-state system where the excited state is reached by inelastic scattering and has a sufficiently long lifetime that an associated elastic conductance is measured by subsequent tunneling electrons. The model reproduces both gap-like and NDR features and can provide information on inelastic channel strengths and residence times even in cases where direct resolution of two-state noise is limited by instrumental bandwidth.

Experiments were performed using ultra-high vacuum STMs operating at temperatures of  $T=5\text{K}$  and  $2.5 < T < 18\text{K}$ . In this temperature range,  $dI/dV$  spectra remain qualitatively unchanged. Data presented here were taken at  $T=5\text{K}$ . Clean surfaces of single-crystal Cu(111) were prepared by Ar sputtering and annealing to 600°C. After transferring the Cu crystal to the cold STM, the polycrystalline Ir tip was positioned over a clean terrace and  $dI/dV$  spectra were recorded with a lock-in amplifier by adding a modulation to the sample voltage  $V$ . H<sub>2</sub> gas was then admitted to the room-temperature UHV chamber ( $P_{\text{H}_2} \sim 1\text{E-}8$  Torr) through a leak valve, producing a constant flux of H<sub>2</sub> cryopumped by the low-temperature section containing the STM. Because direct line-of-sight to the surface was blocked by a mechanical shutter held at  $T=5\text{K}$ , we expect the H<sub>2</sub> to be cold prior to adsorption. Previous studies indicate that H<sub>2</sub> is only weakly bound to cold, noble metal surfaces by van der Waals forces (physisorption) (6,7).

Figure 1(a) shows the evolution of  $dI/dV$  spectra that occurs with  $H_2$  exposure. Spectra taken with  $<870$ min exposure are unchanged from the clean Cu surface. A gap-like feature then suddenly appears with conductance peaks at  $V_{\text{gap}}=80\text{mV}$  that are symmetric about  $V=0$  [Fig. 1(b)]. Figure 1(a) shows that  $V_{\text{gap}}$  increases and the conductance peaks broaden with increasing  $H_2$  exposure, until the gap-structure loses visibility for  $V_{\text{gap}}>200\text{mV}$ . With additional exposure, a feature exhibiting negative differential resistance emerges [Figs. 1(a,c)]. Dips in  $dI/dV$  first occur at  $V_{\text{ndr}}=20\text{mV}$  before broadening and shifting toward higher voltage in a similar fashion to the gap-like feature.

Owing to the mobility of physisorbed  $H_2$ , we are unable to directly observe single  $H_2$  molecules in our STM images, making it difficult to estimate the surface coverage as a function of exposure. For long exposures ( $> 2000$ min), STM images reveal ordering of  $H_2$  beginning around surface adsorbates and step edges that is incommensurate with the underlying Cu lattice. The ordered layer eventually grows to cover entire terraces; by this time the gap-like and NDR features have broadened and shifted considerably ( $V_{\text{gap}} > 200\text{mV}$ ,  $V_{\text{ndr}} > 75\text{mV}$ ), leaving unchanged the small dip at  $V=0$  that is visible in Fig. 1(c). Based on comparable overlayers of physisorbed rare gases (8), it is likely that gap-like and NDR features occur at sub-monolayer  $H_2$  coverage.

Conductance spectra depend on the tip-sample separation, which can be parametrized by the junction resistance  $R$  (decreasing  $R$  by one decade moves the tip  $\sim 0.1\text{nm}$  closer to the surface). For these measurements, we stabilized the  $H_2$  coverage by closing the leak valve when the gap-like feature first becomes visible.  $V_{\text{gap}}$  continues to shift at a reduced rate for several hours afterwards, but eventually settles to a constant value. Figure 2(a) shows that while only the gap-like feature is visible at  $R > 20\text{M}\Omega$ , NDR emerges for  $R < 10\text{M}\Omega$ , so that both features can occur in the same spectrum. Data taken at  $R=10\text{M}\Omega$  during the course of Fig. 1 indicate that the NDR and gap-like features appear concurrently with  $H_2$  exposure. This suggests that tip proximity to the surface and higher coverage both enable the transition responsible for the NDR feature.  $V_{\text{ndr}}$  and  $V_{\text{gap}}$  are typically constant for  $1\text{M}\Omega < R < 1\text{G}\Omega$ , but shift toward low voltage for  $R < 1\text{M}\Omega$  [Fig. 2].

There is often noise present in the conductance peaks of the gap-like feature that provides information on the transition occurring at  $V_{\text{gap}}$ . We can directly resolve this noise in the tunnel current by turning off the voltage modulation and holding the tip-sample separation constant. Fig. 3(a) demonstrates that the noise results from repeated switching between two states. The system resides in a ground state for  $V < V_{\text{gap}}$  and an excited state for  $V > V_{\text{gap}}$ . For  $V \sim V_{\text{gap}}$ , either state is occupied with equal probability. The conductances of ground ( $\sigma_0$ ) and excited ( $\sigma_1$ ) states are independent of voltage, indicating that nonlinearities in  $dI/dV$  solely result from the switching behavior. We calculate the probability of residence ( $n_0, n_1$ ) in each state at a given voltage using the relations:

$$\bar{\sigma} = n_0\sigma_0 + n_1\sigma_1 \quad (1)$$

$$n_0 + n_1 = 1, \quad (2)$$

where  $\bar{\sigma}$  is the time-averaged conductance. The coincidence of  $V_{\text{gap}}$  with changes in  $n_1(V)$  [Fig. 3(b)] indicates that conductance peaks occur as the predominant state of the system changes from the ground to excited state.

To learn more about the mechanism for transitions, we studied the residence times in ground ( $t_0$ ) and excited ( $t_1$ ) states as a function of current by compiling histograms of residence probability versus time [Fig. 3(c)]. The probability distribution can be well fit by a single exponential whose decay constant is the residence time. The dependence of residence times on current in Fig. 3(c) shows that the transition rates between states increase proportionately with the number of available tunneling electrons. This suggests that transitions are driven by inelastic scattering, which is also consistent with the symmetry of  $dI/dV$  spectra about  $V=0$ .

The tunneling current through a junction that can switch between two states is the sum of contributions from elastic and inelastic conductance channels. We assume that the tip and sample densities of states are constant over the voltage range of interest. Inelastic conductance channels transfer the junction from state  $0$  to state  $1$  with conductance  $\sigma_{01}$  or vice versa ( $\sigma_{10}$ ), provided that the sample voltage exceeds threshold values  $V_{01}$  and  $V_{10}$  respectively [Fig. 4(a), inset]. If we exclude spontaneous excitation into state  $1$ , the tunneling current is:

$$I(V) = (n_0\sigma_0 + n_1\sigma_1)V + (n_0\sigma_{01}(V - V_{01}) + n_1\sigma_{10}(V - V_{10})) \quad \text{for } V \geq V_{01}, \quad (3)$$

$$I(V) = \sigma_0 V \quad \text{for } V < V_{01}.$$

For clarity, we consider only  $V \geq 0$  with the understanding that  $I(V)$  should be antisymmetric about  $V=0$ . The residence probability in the excited state is:

$$n_1 = \frac{\Gamma_{01}}{\Gamma_{01} + \Gamma_{10}} = \frac{\sigma_{01}(V - V_{01})}{\sigma_{01}(V - V_{01}) + \sigma_{10}(V - V_{10}) + eS_{10}} \quad \text{for } V \geq V_{01}, \quad (4)$$

$$n_1 = 0 \quad \text{for } V < V_{01}.$$

Here  $\Gamma$ 's represent the total transition rates between states  $0$  and  $1$ , and  $S_{10}$  is the spontaneous relaxation rate from state  $1$ . After substitutions using Eqs. 2 and 4, differentiation of Eq. 3 gives an expression of the form:

$$dI/dV = A + \frac{B}{(1 + (V - V_{01})/V^*)^2} \quad \text{for } V \geq V_{01}, \quad (5)$$

$$dI/dV = \sigma_0 \quad \text{for } V < V_{01},$$

where  $A$ ,  $B$  and  $V^*$  are voltage-independent functions of the seven parameters in the model:  $\sigma_0, \sigma_1, \sigma_{01}, \sigma_{10}, V_{01}, V_{10}, S_{10}$  (9). Figure 4(a) shows that Eq. 5 produces a gap-like feature with conductance peaks at  $V=V_{01}$  when  $\sigma_1 > \sigma_0$ .  $V^*$  sets the decay of  $dI/dV$  from the extremum at  $V=V_{01}$ ,  $A$  is equal to the asymptotic conductance as  $V \rightarrow \infty$  and the sum  $A+B$  is equal to the conductance at  $V=V_{01}$ . Eq. 5 instead produces dips in  $dI/dV$  when  $\sigma_0 > \sigma_1$  (5, 10). Although transition rates are usually faster than can be resolved with the STM, two-state noise has been measured at  $V_{\text{ndr}}$ , verifying that the NDR feature results from switching where  $\sigma_0 > \sigma_1$ . Such noise can emerge at low junction resistance [e.g.  $R=100\text{k}\Omega$  in Fig. 2(a)], indicating that very close proximity to the surface may act to decrease transition rates.

The sharp onset and more gradual decay of the peaks/dips in  $dI/dV$  spectra can be physically understood as a saturation effect. When increasing  $V$  from zero bias, an inelastic path becomes available at  $V = V_{01}$ , suddenly increasing  $n_1$  and thus producing a change in  $dI/dV$ . For  $V > V_{01}$ ,  $dI/dV$  decreases from the extremal value as  $dn_1/dV$  approaches zero. The model may also be applicable to a previous study of NDR where a similar lineshape was observed (5); a host of other spectral features are possible

depending on choices of model parameters. In the limit that  $\Gamma_{10} \gg \Gamma_{01}$ , Eq. 5 reduces to conventional inelastic electron tunneling spectroscopy, where residence in an excited vibrational state is negligible under typical conditions.

It is necessary to introduce broadening to Eq. 5 in order to fit the experimental data. Sources of broadening may include intrinsic uncertainty in the excitation energy  $eV_{01}$  and dynamic fluctuations in local coverage due to the mobility of physisorbed  $H_2$ . Because these sources are difficult to quantify, we empirically convolve Eq. 5 with a Gaussian distribution about  $V_{01}$ . The choice of standard deviation is based on matching the transition region just below  $V_{01}$ , as this region is infinitely sharp in the model. We treat gap-like and NDR features as independent two-state systems, assigning  $V_{01}$  to either  $V_{\text{gap}}$  or  $V_{\text{ndr}}$  as required.

Figure 3(b) includes a calculated  $dI/dV$  curve chosen to fit the experimental data (11). While agreement between calculation and data is good, we note that  $dI/dV$  data alone cannot constrain all seven parameters. Because transition rates are slow compared to rates for elastic tunneling, the parameters  $S_{10}$ ,  $\sigma_{10}$ , and  $\sigma_{01}$  are not uniquely determined and can only be constrained by measurements of  $t_1$  and  $t_0$  from two-state noise (12). The curve for  $n_1(V)$  in Fig. 3(b) was calculated using identical parameters from the fit to  $dI/dV$ . The saturation of  $n_1$  near unity indicates that the inelastic conductance channel  $\sigma_{10}$  is weak compared to  $\sigma_{01}$ .

We usually find that identical fits to  $dI/dV$  data can be produced with or without  $\sigma_{10}$ . Thus it is primarily through analysis of residence times [e.g. Fig. 3(c)] that the existence of  $\sigma_{10}$  is inferred. When two-state noise is not visible due to transition rates that exceed the instrumental bandwidth, it is difficult to determine whether relaxation from the excited state is inelastically driven or spontaneous. If we assume the latter dominates in these cases and set  $\sigma_{10}=0$ , we obtain simpler expressions for  $A$ ,  $B$  and  $V^*$ :

$$A = \sigma_1, B = (V_{01}/V^* - 1)(\sigma_1 - \sigma_0) + \sigma_{01}, \text{ with } V^* = eS_{10}/\sigma_{01} = e/(\sigma_{01} t_1). \quad (6)$$

If  $\sigma_{01}$  is much smaller than the first term in  $B$ , fits to  $dI/dV$  using Eq. 6 only yield the ratio  $S_{10}/\sigma_{01}$ . This is typically the case for NDR data [Fig. 4(b)]. Transition rates well outside the instrumental bandwidth can also occur at  $V_{\text{gap}}$ . The fit in Fig. 4(c) is such that  $\sigma_{01}$  is comparable to the first term in  $B$ , so that  $\sigma_{01}$  and  $S_{10}$  are uniquely determined,

giving an excited state residence time of  $1/S_{10}=t_l=2.2\text{ns}$ . While it is unclear if the assumption  $\sigma_{10}=0$  is justified for these data, this example illustrates that the model can provide information on residence times even when two-state noise is not directly resolved.

In Ref. (5), NDR resulted from changes in molecular conformation states effected by inelastic excitation of vibrational modes. Previous studies have measured the H-H stretch at 510meV for physisorbed  $\text{H}_2$  and 464meV for  $\text{H}_2$  chemisorbed at step edges on Cu(510) (13). Rotational transitions occur at 45/73meV for physisorbed para/ortho- $\text{H}_2$  and 31/61meV for chemisorbed para/ortho- $\text{H}_2$  (13). Vibrations of  $\text{H}_2$  in the physisorption potential well on Cu(100) occur at 9meV (7). In  $\sim 20$  independent repetitions starting with a clean Cu surface,  $V_{\text{gap}}$  begins in the range 25-90mV before shifting to  $V_{\text{gap}}>200\text{mV}$  with increased coverage.  $V_{\text{ndr}}$  more reliably begins at  $11\pm 2\text{mV}$  and shifts to  $V_{\text{ndr}}>75\text{mV}$ . Similar values were observed for HD and  $\text{D}_2$ , although it is difficult to establish whether small isotope shifts occur. While some of the rotational or vibrational modes fall within these ranges of values, it is unlikely that such modes would exhibit the variability or the dependence on coverage observed here.

Conductance measurements of single  $\text{H}_2$  molecules in the point contact regime have revealed a longitudinal vibrational mode at 64meV for  $\text{H}_2$  bound between Pt electrodes (14). While we cannot rule out possible correspondence with  $V_{\text{gap}}$ , we note that the contact geometry and electrode separation are quite different in our STM measurements. We instead speculate that the gap-like and NDR features reflect transitions of  $\text{H}_2$  between different binding sites at the tip apex [Fig. 4(d)]. Experiments and total energy calculations indicate that  $\text{H}_2$  chemisorption is favorable at the low-coordination sites of step edges, with potential well depths less than 100meV for Cu(510) (13,15). This suggests that stable binding of  $\text{H}_2$  to low-coordination sites on the tip may be possible. We find that the shape and position of gap-like and NDR features can significantly change when the atomic structure at the tip apex is perturbed, which may explain the variability of gap-like and NDR features. The identity of atoms at the tip apex is generally unknown, though we expect that tip-preparation via contact with the surface results in a transfer of surface atoms to the tip apex. We have also observed NDR features on Cu(001), Ni(110), CO/Cu(111), NiAl(110), Pt(111), Ag(111) and on Cu(111) with a



tip terminated by a CO molecule. However, gap-like features have only been found on Cu(001) and Al<sub>2</sub>O<sub>3</sub>/NiAl(110), suggesting that the gap-like feature is more dependent on the identity of atoms at the tip apex. The shifts of  $V_{\text{gap}}$  and  $V_{\text{ndr}}$  with coverage may be qualitatively explained as molecular motion that is hindered by surrounding physisorbed H<sub>2</sub>. The number of molecules involved in the switching is difficult to estimate, although the atomic dimensions of the tunnel junction likely limit this number to a few at most.

We conclude by noting that the data in Fig. 4(c) could readily be mistaken for the quasiparticle excitation spectrum in a BCS superconductor. The results presented here demonstrate that a variety of lineshapes can result simply from inelastically driven transitions in two-state systems, providing opportunities for tailored transport characteristics in potential molecular electronic devices.

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  9.  $A = (\sigma_{01}(\sigma_1 + \sigma_{10}) + \sigma_{10}(\sigma_0 + \sigma_{01})) / (\sigma_{01} + \sigma_{10})$   
 $B = \frac{\sigma_{01}[(\sigma_{01}V_{01} + \sigma_{10}V_{10} - eS_{10})(\sigma_1 - \sigma_0) + 2\sigma_{01}\sigma_{10}(V_{01} - V_{10}) + eS_{10}(\sigma_{01} - \sigma_{10})]}{(\sigma_{10}(V_{01} - V_{10}) + eS_{10})(\sigma_{01} + \sigma_{10})}$   
 $V^\dagger = (\sigma_{10}(V_{01} - V_{10}) + eS_{10}) / (\sigma_{01} + \sigma_{10})$
  10. An NDR feature may also be produced when  $\sigma_1 > \sigma_0$  if  $n_1 \neq 0$  for  $V < V_{01}$ . In such a case, the inelastic channel  $\sigma_{10}$  acts to reduce the probability  $n_1$  once  $V > V_{10}$ , thus switching from a high to low conductance state as required for NDR.
  11. Fit parameters are:  $V_{01}=108\text{mV}$ ,  $V_{10}=70\text{mV}$ ,  $\sigma_0=8.6\text{nA/V}$ ,  $\sigma_1=21\text{nA/V}$ ,  $\sigma_{01}=8\text{pA/V}$ ,  $\sigma_{10}=0.1\text{pA/V}$ ,  $S_{01}=1000\text{ s}^{-1}$ , broadening =  $4.7\text{mV}$ .
  12. Additional studies of  $t_1(V)$  indicate that  $t_1$  increases for  $V > V_{01}$ , suggesting that other mechanisms not included in our model affect transition rates. Possibilities include electric field effects or interaction with surrounding  $\text{H}_2$  molecules.
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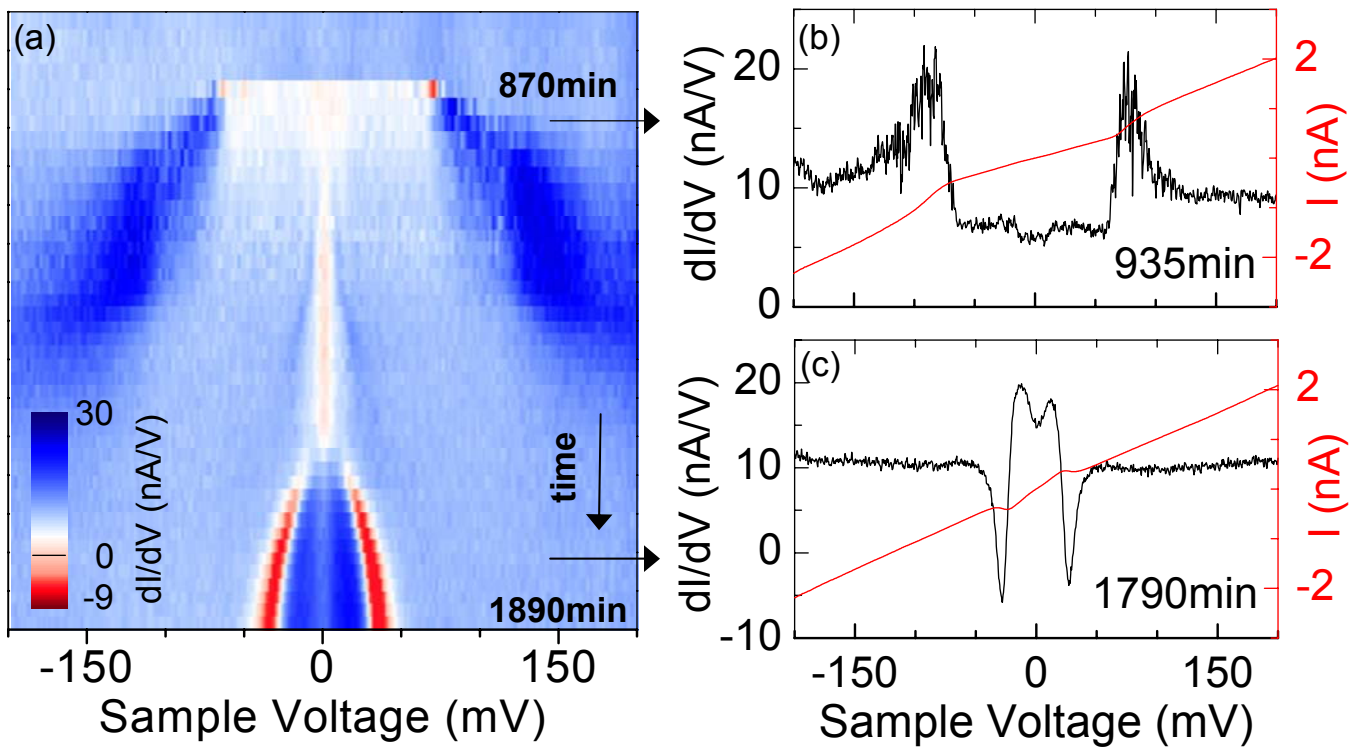


Fig. 1: (a)  $dI/dV$  spectra taken as  $H_2$  coverage increases with time. (b),(c) Linecuts of  $dI/dV$  indicated by the arrows in (a). Shown in red are corresponding  $I(V)$  curves.  $R = 100M\Omega$  ( $V=100mV$ ,  $I=1nA$ ), modulation  $=0.5mV_{rms}$ . Spectra are the average of  $10 \times 1min$  sweeps.

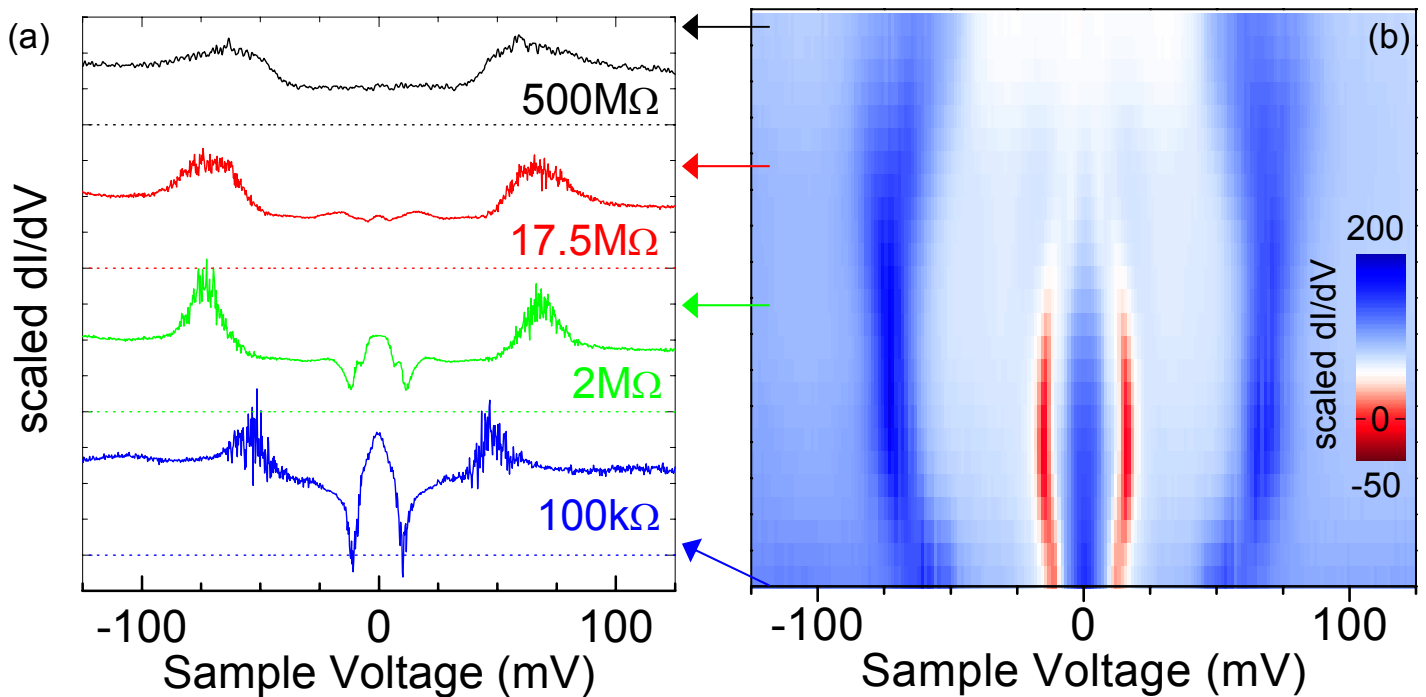


Fig. 2: Emergence of NDR with decreasing junction resistance. All data are scaled by  $R/10\text{M}\Omega$  ( $V=100\text{mV}$ ,  $I=10\text{nA}$ ). (a) Spectra are offset by  $200\text{nA/V}$  for clarity. Dotted lines indicate zero conductance for each scan. Data at  $R=500\text{M}\Omega$  are the average of 5 sweeps, while the others are single sweeps. From top to bottom, RMS modulation =  $2\text{mV}$ ,  $1\text{mV}$ ,  $0.5\text{mV}$ ,  $0.2\text{mV}$ . (b) Complete series for  $500\text{M}\Omega < R < 0.1\text{M}\Omega$ .

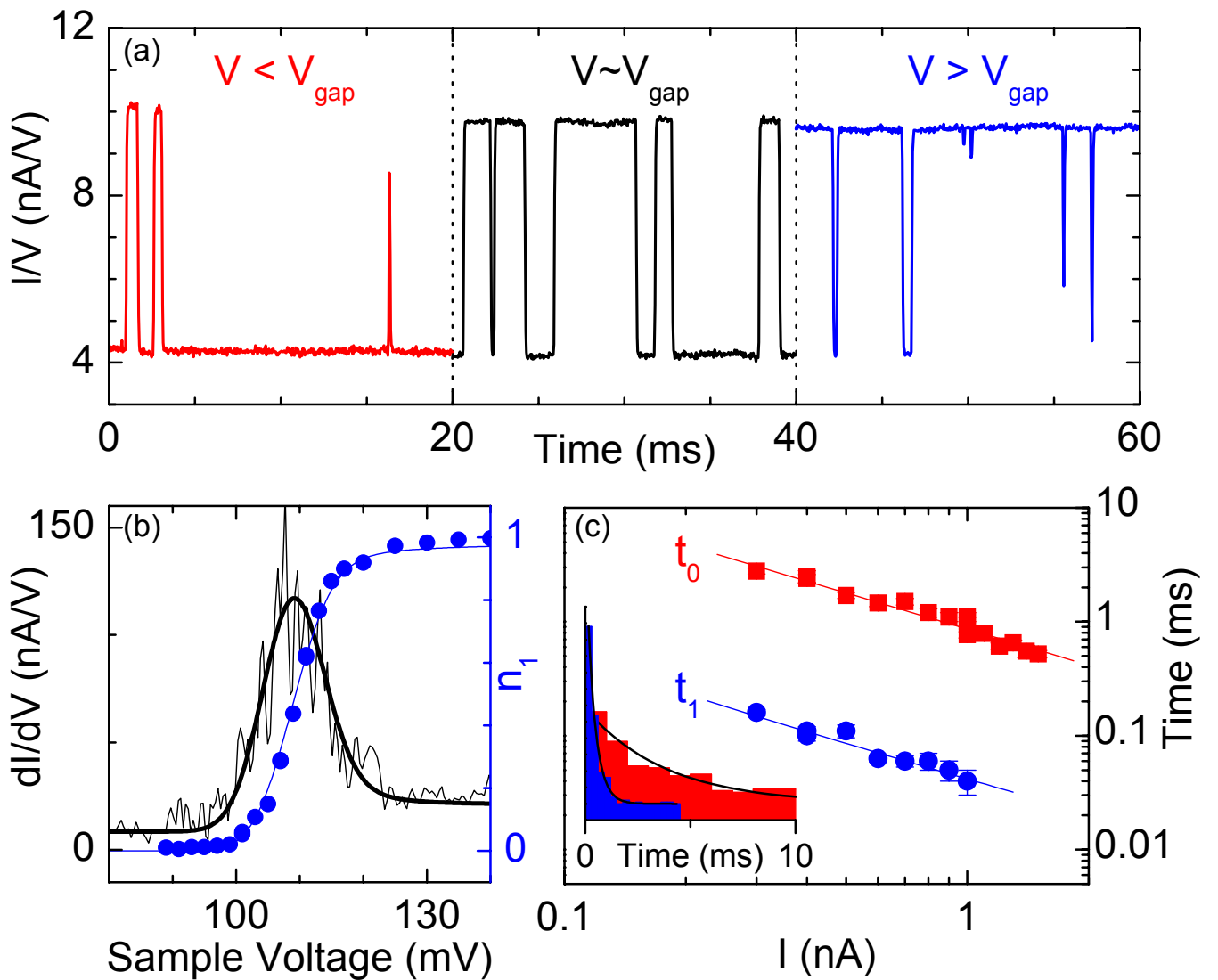


Fig. 3: Two-state noise at  $V_{\text{gap}}$ . (a) Switching in conductance with  $V=95\text{mV}$  (red),  $109\text{mV}$  (black),  $125\text{mV}$  (blue) taken after opening the STM feedback loop at  $V=150\text{mV}$ ,  $I=1.5\text{nA}$ . (b) Left axis:  $dI/dV$  showing  $V_{\text{gap}}=108\text{mV}$ . The solid line is a fit using Eq. 5 and parameters in Ref. (11). Right axis (blue): Residence probability in the excited state. The solid line is calculated using Eq. 4 with identical parameters (11). (c) Inset: histogram of residence probability versus time for ground (red) and excited (blue) states extracted from two-state noise at  $V=110\text{mV}$ ,  $I=0.2\text{nA}$ , along with exponential fits (black lines). Main (log-log scale): Residence times  $t_0$  and  $t_1$  from exponential fits. Lines are fits with slopes of  $-1.0$ . Data were taken shortly after those in (a-b), so that  $V_{\text{gap}}=120\text{mV}$  due to a higher coverage.

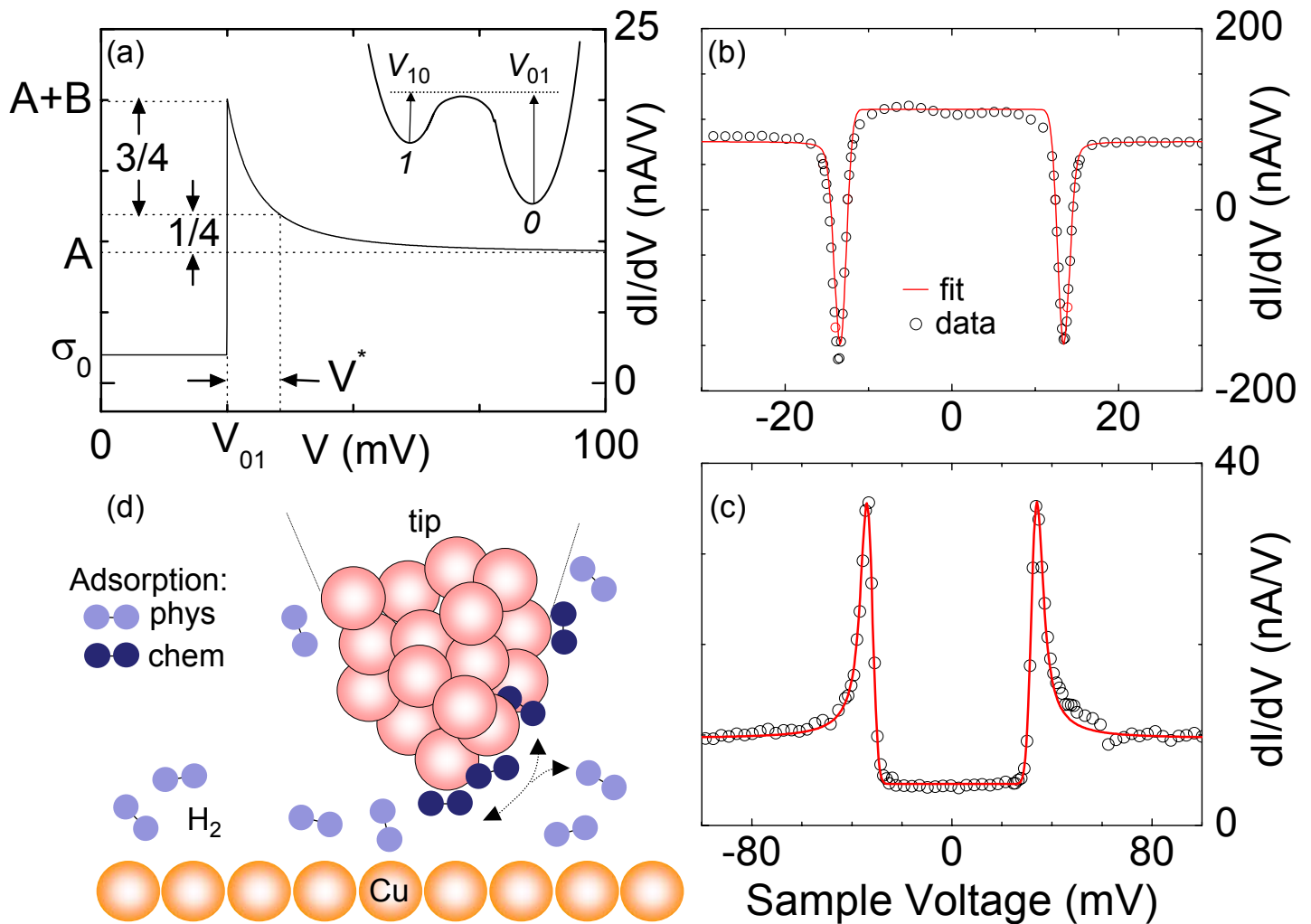


Fig. 4: Model and fits. (a) Calculation of  $dI/dV$  using Eq. 5 with  $\sigma_0=2\text{nA/V}$ ,  $\sigma_1=10\text{nA/V}$ ,  $\sigma_{01}=2\text{nA/V}$ ,  $\sigma_{10}=0.5\text{nA/V}$ ,  $S_{10}=0.1\text{GHz}$ ,  $V_{01}=25\text{mV}$ ,  $V_{10}=5\text{mV}$ . Inset: schematic of two-state system. (b) Data (open symbols) taken for  $H_2/Cu(111)$  with ( $V=10\text{mV}$ ,  $I=1\text{nA}$ ,  $0.5\text{mV}_{\text{rms}}$  modulation, 4 sweeps) and fit (red line) using Eq.6 with ( $\sigma_0 = 110.8\text{nA/V}$ ,  $\sigma_1 = 74.1\text{nA/V}$ ,  $V^*=0.03\text{mV}$ ,  $V_{01}=13.3\text{mV}$ , broadening =  $0.8\text{mV}$ ). (c) Data (open symbols) taken for  $H_2/Cu(001)$  with ( $V=100\text{mV}$ ,  $I=1\text{nA}$ ,  $0.5\text{mV}_{\text{rms}}$  modulation, 20 sweeps) and fit (red line) with ( $\sigma_0 = 4.5\text{nA/V}$ ,  $\sigma_1 = 9.7\text{nA/V}$ ,  $\sigma_{01}=32.2\text{nA/V}$ ,  $t_1=2.15\text{ns}$ ,  $V_{01}=32.2\text{mV}$ , broadening =  $1.8\text{mV}$ ). (d) Schematic of possible adsorption states at the tip apex.